

SPECIAL ED

# Advanced Algebra Solving Inequalities

$$5 + 3x > 21$$



**INCLUDES GOOGLE SLIDES**

*This unit was created with this guy in mind. He has autism and an intellectual disability. He is a non-reader, has a very short attention span, and has a few foundational math skills. With some support, he is able to do this unit and enjoys the challenge. He is my tester!!*



## **COSMIC steps**

*This unit uses the COSMIC steps when solving an equation.*

- 1. Copying/translating the problem*
- 2. Operation choice (addition or subtraction)*
- 3. Subtracting or adding*
- 4. Multiply or divide to get rid of the coefficient*
- 5. Isolate the variable*
- 6. Draw your answer on a number line*

**There are lots of worksheets to practice each step.**

# Advanced Algebra: Inequalities Unit

By

Christa Joy

Special Needs for Special Kids

 $>$     $<$ 
 $\geq$     $\leq$ 

Christa Joy, Special Needs for Special Kids  
The Picture Communication Symbols ©1981–2018 by Tobii Dynavox. All Rights Reserved  
Worldwide. Used with permission. Boardmaker® is a trademark of Tobii Dynavox

## Inequalities

### Table of Contents

Pages	Activity
4-5	Vocabulary board
6-9	Vocabulary cards
10-19	Vocabulary cut and paste
20-23	Key word cards
24-28	COSMIC cards
29-32	Drawing inequalities on the number line
33-37	Identify possible values
38-53	COSMIC worksheet set #1
54-68	COSMIC worksheet set #2
69-78	COSMIC worksheet set #3
79-91	COSMIC worksheet set #4
92-98	Vocabulary Sudoku
99-113	Assessment
114-115	Terms of Use

Also included in this resource as separate files:

- Lesson plans
- Links and directions to digital activities
- PowerPoint (**this is the book in the lesson plan**)
- Voice recorded PowerPoint
- Activities in black and white

*This unit contains over 200 pages of material and 92 google slides. I have a lesson plan to help you make the most of everything in this unit including how to add some group activities.*

# Advanced Algebra: Solving Inequalities Lesson Plan

## Preparation

- Print out a vocabulary board for each student to use throughout unit
  - Laminate or place in page protector
- Book
  - Print out, laminate, and bind
  - OR your students can listen to the pre-recorded version
- Vocabulary cards
  - Print out a set of cards onto cardstock and laminate
  - Make one set for each student and also one for the teacher to use in I Spy games
- Key words cards and COSMIC cards
  - Determine the best format/size for
  - Print onto cardstock and laminate
- Extra Number Lines (included in Identif
  - Print on cardstock and laminate
  - Students can use dry erase marker

## Preassessment (do day 1 before starting lesson)

- Choose the form of the assessment that
- Give the assessment to assess what your
- I cannot emphasize enough how important growth, this preassessment is so important

## Teaching Tips

1. *Color Coding*: this is a really easy way activity. Outline or color in an empty 1 the corresponding picture symbols the task.
  - a. For more info, read more here: <https://specialneedsforspecialkid.com/differentiation/>
  - b. I also have a blog post on differentiation: <https://specialneedsforspecialkid.com/3-ways-easily-and-effectively/>

## Day 2

Activity	Notes	Materials
Read or listen to a recording of the book (10 minutes)	<ul style="list-style-type: none"> <li>• Read through the story, asking lots of questions</li> <li>• Continue to make connections between book and vocabulary board</li> </ul>	<ul style="list-style-type: none"> <li>• Book</li> <li>• Vocabulary board</li> </ul>
Vocabulary cards I Spy Game (10 minutes)	<ul style="list-style-type: none"> <li>• I play this game, or variations of it the first few days                             <ul style="list-style-type: none"> <li>◦ Determine how many cards your students can handle in front of them. This can vary, some students may be able to have all the cards, so may only be able to handle a field of 3-5</li> </ul> </li> <li>• Since this is the first time playing this game, I make it easy. Hold up a card, and have students find the matching one and hold it up</li> <li>• Discuss relevant points on the card                             <ul style="list-style-type: none"> <li>◦ You can also play this game in this manner having them find the symbol on their vocabulary board</li> </ul> </li> </ul>	<ul style="list-style-type: none"> <li>• Vocabulary cards (student set and teacher set)</li> <li>• Vocabulary board</li> </ul>
Key words review (5 minutes)	<ul style="list-style-type: none"> <li>• Review the key word cards</li> </ul>	<ul style="list-style-type: none"> <li>• Key words cards</li> </ul>
Intro COSMIC cards (10 min)	<ul style="list-style-type: none"> <li>• Determine which set is going to be best for your students.</li> <li>• This plan spends 3 days focused on each step (except step 2&amp;3 are combined into one)</li> <li>• Talk through the cards and make connections to the book and vocabulary cards and board</li> </ul>	<ul style="list-style-type: none"> <li>• COSMIC cards</li> <li>• Vocabulary board</li> <li>• Vocabulary cards</li> </ul>
Drawing inequalities on the number line (10 minutes)	<ul style="list-style-type: none"> <li>• Do one or more of the worksheets where students draw the inequality on the number line.</li> <li>• Watch for the open/closed circles depending on the sign</li> <li>• Ask student to verbalize or point to possible values of X</li> </ul>	<ul style="list-style-type: none"> <li>• Worksheet</li> </ul>
Sharing (10 minutes)	<ul style="list-style-type: none"> <li>• Each student shares one of their finished worksheet with the group using the communication method of their choice</li> </ul>	<ul style="list-style-type: none"> <li>• Completed worksheets</li> <li>• Communication devices</li> </ul>

## Quick Look

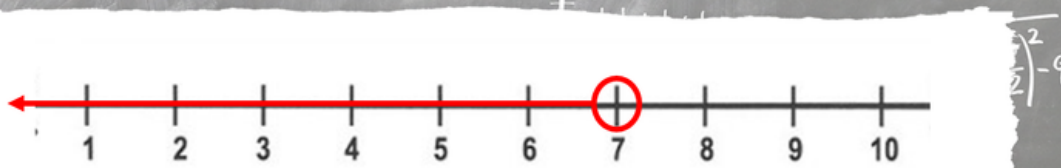
Day	Activity	Day	Activity	Day	Activity
1	<ul style="list-style-type: none"> <li>• Book</li> <li>• Intro vocab cards</li> <li>• Intro Key words cards</li> </ul>	7	<ul style="list-style-type: none"> <li>• Book</li> <li>• Vocab cards activity</li> <li>• Worksheet set 1 practice</li> </ul>	13	<ul style="list-style-type: none"> <li>• Book</li> <li>• Vocab cards activity</li> <li>• Worksheet set 3 practice</li> </ul>
2	<ul style="list-style-type: none"> <li>• Book</li> <li>• Vocab cards activity</li> <li>• COSMIC cards</li> <li>• Drawing on a number line</li> </ul>	8	<ul style="list-style-type: none"> <li>• Book</li> <li>• Vocab cards activity</li> <li>• Worksheet set 1 practice</li> </ul>	14	<ul style="list-style-type: none"> <li>• Book</li> <li>• Vocab cards activity</li> <li>• Worksheet set 2 practice</li> </ul>
	<ul style="list-style-type: none"> <li>• Book</li> </ul>	9	<ul style="list-style-type: none"> <li>• Book</li> <li>• Vocab cards activity</li> <li>• Worksheet set 1 practice</li> </ul>	15	<ul style="list-style-type: none"> <li>• Book</li> <li>• Vocab cards activity</li> <li>• Worksheet set 2 practice</li> </ul>
		10	<ul style="list-style-type: none"> <li>• Book</li> <li>• Vocab cards activity</li> <li>• Worksheet set 2 practice</li> </ul>		
		11	<ul style="list-style-type: none"> <li>• Book</li> <li>• Vocab cards activity</li> <li>• Worksheet set 2 practice</li> </ul>		
		12	<ul style="list-style-type: none"> <li>• Book</li> <li>• Vocab cards activity</li> <li>• Worksheet set 2 practice</li> </ul>		
				15	

The lesson plans contain:

- Preparation needed
- Overall tips for teaching students with significant needs
- Daily flow of the lesson including individual and group activities

The easiest way to visualize this is to put it on a number line.

$$x < 7$$



So, if you see the equation  $x < 7$  then you know that  $x$  could be any number that is less than 7. It could be 0, 1, 2, 3, 4, 5, 6 or even a negative number.

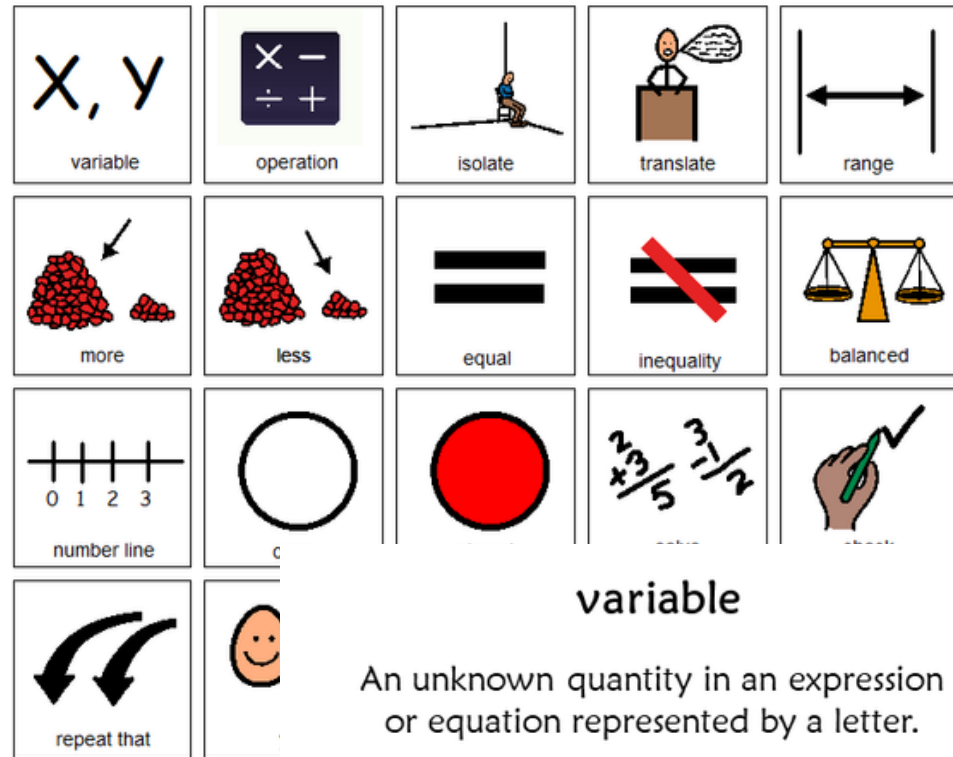
$$x < 7$$

-1?    1?    2?    4?  
-2?    0?    3?    5?    6?

There is a 36 page book using simple text and photos. It walks students through the steps to solving inequalities using the COSMIC steps.

- PowerPoint
- voice-recorded PPT
- mp4 movie format

# Vocabulary



The Picture Worlds

## variable

An unknown quantity in an expression or equation represented by a letter.

# X, Y

## equation

Expression with one of the following signs:  
= < > ≤ ≥.



## inequality

An expression that does not have a single answer; uses one of the following symbols: < > ≤ ≥.



## isolate

To solve the equation so the variable is *by itself* on one side of the sign.



There is a vocabulary board (used for class discussion) and vocabulary cards with cut and paste activities.

# Key word cards

<p><b>Addition</b></p> <ul style="list-style-type: none"><li>• Add</li><li>• Addition</li><li>• Sum of</li><li>• Plus</li><li>• Increase by</li><li>• More than</li><li>• Total</li></ul> <p><b>+</b></p>	<p><b>Subtraction</b></p> <ul style="list-style-type: none"><li>• Subtract</li><li>• Decrease by</li><li>• Difference</li><li>• Less than</li><li>• Take away</li><li>• Minus</li></ul> <p><b>-</b></p>
<p><b>Multiplication</b></p> <ul style="list-style-type: none"><li>• Times</li><li>• Product</li><li>• Multiplied by</li><li>• Per</li><li>• Each</li></ul> <p><b>×</b></p>	<p><b>Division</b></p> <ul style="list-style-type: none"><li>• Divide</li><li>• Separate</li><li>• Quotient</li><li>• Divided by</li><li>• Split into</li></ul> <p><b>÷</b></p>

There are 4 cards (in different sizes) that students can refer to looking for key words when solving equations.



# COSMIC cards

There are cards for students to refer to listing the steps in the COSMIC method.

They come with and without pictures.

**COSMIC**

- 1. Copy/translate the problem
- 2. Operation choice
- 3. Subtract or add
- 4. Multiply or divide IF coefficient
- 5. Isolate the variable
- 6. Draw you answer on the number line

**COSMIC**


- 1. Copy/translate the problem
- 2. Operation choice
- 3. Subtract or add
- 4. Multiply or divide IF coefficient
- 5. Isolate the variable
- 6. Draw you answer on the number line

©Christa Joy, SNSK  
The Picture Communication Symbols ©1981–2019 by Tobii Dynavox. All Rights Reserved  
Worldwide. Used with permission. Boardmaker® is a trademark of Tobii Dynavox

**COSMIC**

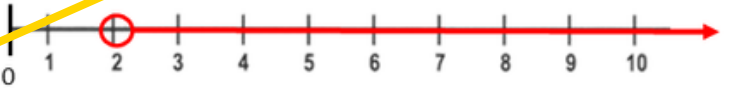
5. Isolate the variable

\*\*\*Get the X on one side of the equal sign\*\*\*



**COSMIC**

6. Draw you answer on the number line



©Christa Joy, SNSK  
The Picture Communication Symbols ©1981–2019 by Tobii Dynavox. All Rights Reserved  
Worldwide. Used with permission. Boardmaker® is a trademark of Tobii Dynavox

Laminate so students can check off when complete.

Read each problem and translate into an inequality.

1. A number increased by six is less than twenty
2. A number decreased by four is more than five
3. Eight more than a number is greater than or equal to ten
4. A number minus ten is less than or equal to fifteen
5. Seven take away a number is greater than nine

# COSMIC step #1

Read each problem and **circle** the correct inequality.

1. A number increased by fourteen is less than twenty

$$X+5 \leq 7$$

$$10-x > 20$$

$$X+14 < 20$$

2. A number decreased by six is greater than or equal to fourteen

$$X-6 \geq 14$$

$$7-x > 14$$

$$X+6 < 14$$

3. Ten more than a number is less than or equal to fifteen

$$X+1 \geq 8$$

$$X+10 \leq 15$$

$$X-4 < 15$$

4. A number minus one is less than thirteen.

$$X-7 \leq 23$$

$$1+x > 13$$

$$X-1 < 13$$

5. Nine take away a number is greater than one

$$9-x > 1$$

$$12+x < 18$$

$$X-17 \geq 25$$

There are 15 worksheets where students will practice **copying and translating** the problem into an algebraic equation.

Students can write in answers or cut and paste answers provided on a separate page.

# COSMIC step #2

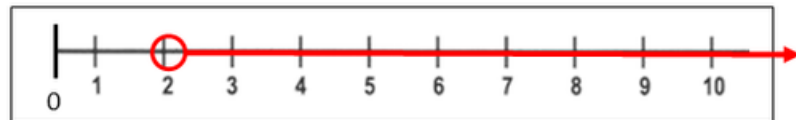
1. Decide if you need to add or subtract from both sides.
2. Circle either the + or - sign.
3. Either add or subtract the correct number of pictures as the first step in isolating the variable on one side.
4. Draw your final answer on the number line. *NOTE: explain to students when graphing on the number line, we are assuming each picture is equal to a value of 1.*

Example:

1

$$x + \cancel{1} + \cancel{1} > \cancel{1} + \cancel{1} + 1 + 1$$
$$- 1 - 1 > 1 + 1$$

$$x > 2$$



Addition/subtraction

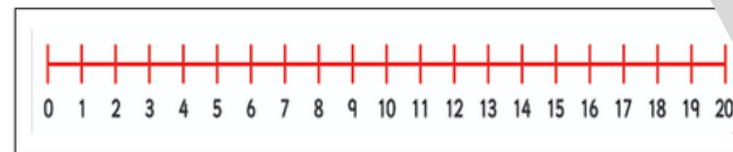
1. Decide if you need to add or subtract from both sides.
2. Circle either the + or - sign.
3. Either add or subtract the correct number as the first step in isolating the variable on one side.
4. Draw your final answer on the number line.

Example:

1

$$x + 2 > -2 - 10$$

$$x > 8$$



There are 4 worksheets where students *will identify the operation* in the equation.

There are 2 using pictures and 2 with numbers.

There is an example (shown here) worked out for you.

## COSMIC step #3

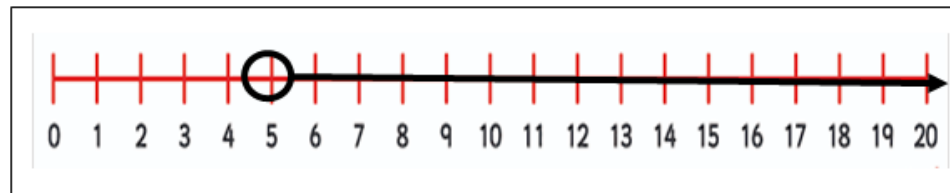
1. Decide if you need to multiply or divide from both sides.
2. Write to the side if you will multiply (x) or divide ( $\div$ ).
3. Circle the coefficient.
4. Either multiply or divide by the correct coefficient as a step in isolating the variable on one side.
5. Draw your answer on the number line.

Example:

1  
x

$$5X > 25$$
$$\div 5 > \div 5$$

$$X > 5$$



There are 4 worksheets where students will practice which operation they need to do in order to *eliminate a coefficient*.

There is an example (shown here) worked out for you.

# COSMIC step #4

1. Translate the problem.
2. Decide if you need to add/subtract.
3. Write the new problem.
4. Decide if you need to multiply/divide.
5. Is the variable isolated? Draw your answer on the number line.

Example: Two times a number plus ten is greater than twenty.

$$2X + 10 > 20$$

1

+

$$\begin{array}{r} 2X + 10 > 20 \\ -10 \quad -10 \end{array}$$

2

-

$$2X > 10$$

3

X

$$\begin{array}{r} 2X > 10 \\ \div 2 \quad \div 2 \end{array}$$

4

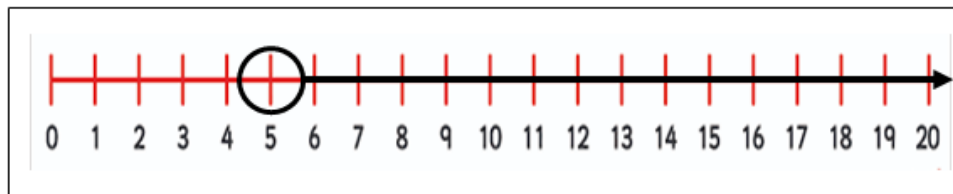
÷

yes

$$X > 5$$

5

no



There are 10 worksheets where students will practice *isolating the variable*.

There is an example (shown here) worked out for you.

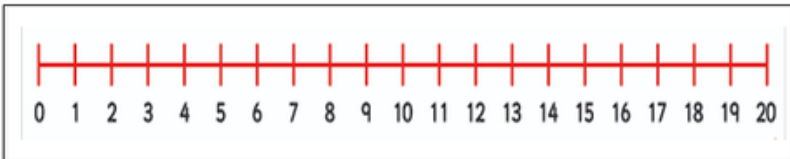
1. Decide if you need to add or subtract from both sides.
2. Circle either the + or - sign.
3. Either add or subtract the correct number as the first step in isolating the variable on one side.
4. Draw your final answer on the number line.

Example:

1

$$x + 2 > 10$$

$$x > 8$$



# COSMIC step #5

1. Decide if you need to multiply or divide from both sides.
2. Write to the side if you will multiply (x) or divide (÷).
3. Circle the coefficient.
4. Either multiply or divide by the correct coefficient as a step in isolating the variable on one side.
5. Draw your answer on the number line.

Example:

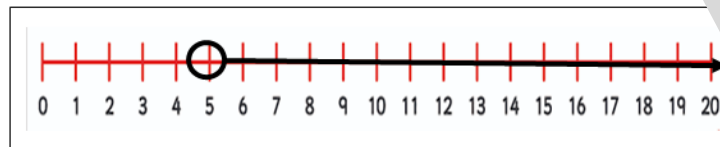
1

X

$$5x > 25$$

$$\div 5 > \div 5$$









$$x > 5$$







There are 11 worksheets where students will draw all possible answers on a number line.

There is an example worked out for you.



# Inequalities

<b>X, Y</b> variable	 translate	<del>=</del> inequality	 isolate	$\geq$ greater than or equal to	$\leq$ less than or equal to
 isolate				 translate	<del>=</del> inequality
	 isolate	 translate	$\geq$ greater than or equal to		<b>X, Y</b> variable
$\geq$ greater than or equal to	<del>=</del> inequality	$\leq$ less than or equal to	<b>X, Y</b> variable	 isolate	
	$\leq$ less than or equal to			<b>X, Y</b> variable	
 translate	<b>X, Y</b> variable				

Place the following images in the empty squares on the previous page, completing the sudoku puzzle.

$\geq$ greater than or equal to	$\geq$ greater than or equal to	$\leq$ less than or equal to	$\leq$ less than or equal to
$\leq$ less than or equal to	<b>X, Y</b> variable	 isolate	 isolate
<del>=</del> inequality	<del>=</del> inequality	 translate	 translate

# Inequalities

	$>$ greater than	 translate	$<$ less than
		$>$ greater than	
	<del>=</del> inequality		
 translate			

There is a Sudoku puzzle in this unit as well. This is a great way to work with the new vocabulary!!

There are 2 versions plus answer keys.

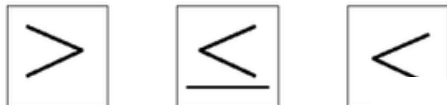
1. True or False. You solve an inequality the same way you solve a linear equation.



2. Which symbol means greater than OR equal to?



3. Which symbol means less than?



4. How would you draw this on a number line?

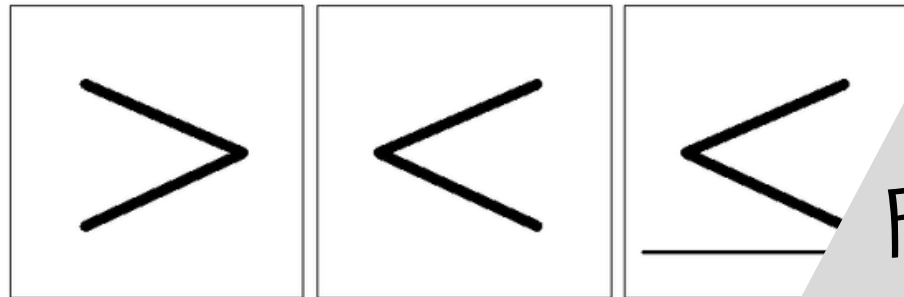


5. Circle all the possible answers for

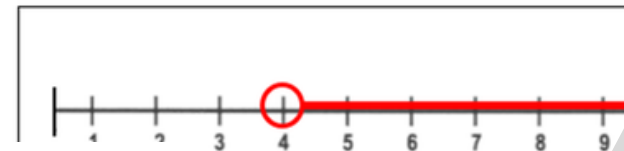


Print onto cardstock or mount on index cards. Cut pictures apart and show student answer choices for each question.

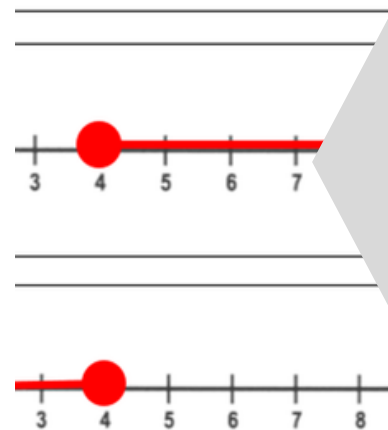
Q 3



Q 4



Version 3



1. True or False. You solve an inequality the same way you solve a linear equation.
  - A. True
  - B. False
  - C. I don't know
2. Which symbol means greater than OR equal to?
  - A. <
  - B. >
  - C. ≥
3. Which symbol means less than?
  - A. >
  - B. ≤
  - C. <
4. How would you draw this on a number line?  $X > 4$



5. Circle all the possible answers for  $Y \leq 5$ 
  - A. 0
  - B. 5
  - C. 7
  - D. 3
  - E. 2
  - F. 9
6. Translate this inequality: a number is less than or equal to five.
  - A.  $X < 5$
  - B.  $Y > 5$
  - C.  $X \leq 5$

FINALLY the assessment!! There are 3 versions.


- 10 questions with 3 picture choices for each question
- cut out the answer choices and glue them on index cards
- traditional multiple choice

Answer key included.



Watch the  
movie on  
Inequalities

Then, we can begin isolating the variable on one side of the equation.



$x^2 + p$

$12$

$2a$

$-x$

$\frac{1}{2} = -\frac{1}{2}$

$\sin$

Christa Joy, Special Needs for Special Kids

This unit also has  
digital activities.  
There is a movie  
version of the book  
students can listen to  
read aloud.

# Great for review

$X/3 \geq 4$

[Blank box for student response]

[Blank box for student response]



$10X \leq 20$

[Blank box for student response]

[Blank box for student response]



## COSMIC 3

1. Decide if you need to multiply or divide from both sides.
2. Write to the side if you will multiply (x) or divide ( $\div$ ).
3. Either add or subtract as the first step in isolating the variable on one side.
4. Draw the answer on the number line.

$\times$         $\div$

$\div 10$         $\div 10$

$\times 3$         $\times 3$

$X \geq 12$

$X \leq 2$



Christa Joy, Special Needs for Special Kids  
The Picture Communication Symbols ©1981-2019 by Tobii Dynavox. All Rights Reserved  
Worldwide. Used with permission. Boardmaker® is a trademark of Tobii Dynavox

The digital activities have students click and drag their answers. There are 2 sets slides.

# Perfect for all learning levels

A number divided by two minus four is less than three

1


2

3

4


5

yes  
no



## COSMIC 4

1. Translate the problem.
2. Decide if you need to add/subtract.
3. Write the new problem.
4. Decide if you need to multiply/divide.
5. Is the variable isolated? Circle the answer.
6. Draw the answer on the number line.



Christa Joy, Special Needs for Special Kids  
The Picture Communication Symbols ©1981-2019 by Tobii Dynavox. All Rights Reserved  
Worldwide. Used with permission. Boardmaker® is a trademark of Tobii Dynavox

The second set of slides is differentiated using either color or numbers for students to match to.

*This resource comes in a zipped folder. You will need to unzip the folder to access all the contents which include:*

- *Lesson plan*
- *Inequalities activities in BW*
- *Inequalities activities in color*
- *Solving Inequalities book (PowerPoint) to use with activities*
- *Links and directions to digital activities*

Save money and get this unit in a bundle with more advanced algebra units.

**Algebra Bundle**

